

2 0 2 5

(NEP—2020)

(5th Semester)

MATHEMATICS (MAJOR3/MINOR)**(Astronomy)***Full Marks : 75**Time : 3 hours**The figures in the margin indicate full marks for the questions***(SECTION : A—OBJECTIVE)***(Marks : 10)*Put a Tick mark against the correct answer in the box provided : 1×10=10**1.** The sides of spherical triangle are

- | | |
|--|---|
| (a) less than 180° <input type="checkbox"/> | (b) greater than 180° <input type="checkbox"/> |
| (c) equal to 180° <input type="checkbox"/> | (d) None of the above <input type="checkbox"/> |

2. Each angle of a spherical equilateral triangle is

- | | |
|---|--|
| (a) equal to 60° <input type="checkbox"/> | (b) greater than 60° <input type="checkbox"/> |
| (c) less than 60° <input type="checkbox"/> | (d) None of the above <input type="checkbox"/> |

3. Obliquity of ecliptic is equal to

- | | |
|---|---|
| (a) 30° <input type="checkbox"/> | (b) 60° <input type="checkbox"/> |
| (c) 45° <input type="checkbox"/> | (d) $23^\circ 27'$ <input type="checkbox"/> |

4. The zenith Z is the pole of
 (a) ecliptic (b) horizon
 (c) celestial equator (d) None of the above
5. Hour-angle of the zenith is
 (a) 180° (b) 90°
 (c) 60° (d) 0°
6. On summer solstice, longitude of the sun is
 (a) 0° (b) 90°
 (c) 180° (d) 270°
7. The difference between local mean time and hour-angle of the mean sun is
 (a) 6 hours (b) 9 hours
 (c) 12 hours (d) 18 hours
8. At a place of latitude 45° (north) azimuth A of star of declination 30° when rising is
 (a) 30° (b) 45°
 (c) 60° (d) 90°
9. If the observed zenith distance of a star is z , then the parallax of the star varies as
 (a) $\sin z$ (b) $\cos z$
 (c) $\sin 2z$ (d) $\tan z$
10. During solar eclipses the moon must be in
 (a) conjunction (b) opposition
 (c) quadrature (d) None of the above

(SECTION : B—SHORT ANSWERS)

(Marks : 15)

Answer *five* questions, taking at least *one* from each Unit : 3×5=15

UNIT—I

1. In a right angled spherical triangle ABC , $A = 90^\circ$, then show that
 $\cos a = \cos b \cos c$

2. Show that in spherical equilateral triangle ABC , $\sec A = 1 + \sec a$.

UNIT—II

3. A star of declination 30° is observed to attain an altitude of 45° on the prime vertical. What is the latitude of the place of observation?
4. If a is the sun's altitude in the prime vertical at a place in latitude ϕ and L is its longitude, then prove that $\sin^2 \phi = \sin L \sin a \operatorname{cosec} a$.

UNIT—III

5. If the declination of the sun be $12^\circ 30' N$, find the lowest latitude at which twilight lasts all night.
6. Define equation of time.

UNIT—IV

7. Show that the resolved part of aberration of a star α along any great circle arc AB , where $B = 90^\circ$ is $k \cos AB$. A being apex and k coefficient of aberration.
8. Show that the parallax in declination of a planet observed from a place in latitude ϕ vanishes, if $\tan \phi = \tan^2 h \cos \delta$; and h being the planet's declination and hour-angle.

(SECTION : C—DESCRIPTIVE)

(Marks : 50)

Answer *five* questions, taking at least *one* from each Unit :

10×5=50

UNIT—I

1. (a) If A and A' be angles of an equilateral triangle and its polar triangle respectively, then prove that $\cos A = \cos A' \cos A' \cos A$. 5
- (b) If D be the middle point of AB of a spherical triangle ABC , then show that

$$\cos a \cos b = 2 \cos \frac{c}{2} \cos CD \quad 5$$

2. (a) In a spherical triangle ABC , show that

$$\sin b \sin c \cos b \cos c \cos A = \sin B \sin C \cos B \cos C \cos a$$
 5
- (b) Show that in a spherical equilateral triangle ABC , $1 - 2 \cos a = \cot^2 \frac{A}{2}$. 5

UNIT—II

3. Two stars (λ_1, μ_1) and (λ_2, μ_2) have same longitude. Prove that

$$\sin(\lambda_1 - \lambda_2) \tan(\mu_1 \cos \lambda_1 \tan \mu_2 \cos \lambda_2 \tan \mu_1)$$
 10
4. (a) If z_1 and z_2 are zenith distances of a star on the meridian and on the prime vertical respectively, then prove that

$$\cot \mu \operatorname{cosec} z_1 \sec z_2 = \cot z_1$$
 5
- (b) At what latitude the sun sets at 4 PM (of apparent solar time) at the solar solstice? 5

UNIT—III

5. (a) If H be the hour-angle of the sun at rising, then show that

$$2 \cos^2 \frac{H}{2} \sec \mu \sec \delta \cos(\mu - \delta) \text{ and } \tan^2 \frac{H}{2} = \frac{\cos(\mu - \delta)}{\cos(\mu + \delta)}$$
 5
- (b) In north latitude 45° , the greatest azimuth of a star is 45° (east or west). Prove that the star's declination is 60° N. 5
6. Derive Cassini's formula for atmospheric refraction. 10

UNIT—IV

7. Find the effect of aberration on right ascension and declination. 10
8. (a) Where must a star be situated so that effect of the annual parallax is greatest? When is it greatest? 5
- (b) Show that $p = P \sin z$, where z = observed zenith distance, p = geocentric parallax and P = horizontal parallax. 5
